

**ON EDGE IRREGULAR m-BIPOLAR FUZZY GRAPHS**

**Ramakrishna Mankena<sup>1\*</sup>, D Prathap<sup>2</sup> T V Pradeep Kumar<sup>3</sup>, Ch Ramprasad<sup>4</sup>**

<sup>1</sup>Department of Mathematics, Malla Reddy College of Engineering, Hyderabad-500100, India.

<sup>2</sup>Department of Mathematics, CMR Institute of Technology, Bengaluru-560037, India.

<sup>1,3</sup>Department of Mathematics, University College of Engineering, Acharya Nagarjuna University-522510, India.

<sup>4</sup>Department of Mathematics, Vasireddy Venkatadri Institute of Technology, Namburu-522508, India.

E mail ids: <sup>1\*</sup>[rams.prof@gmail.com](mailto:rams.prof@gmail.com), <sup>2</sup>[pratap.d@cmrit.ac.in](mailto:pratap.d@cmrit.ac.in), <sup>3</sup>[pradeeptv5@gmail.com](mailto:pradeeptv5@gmail.com), <sup>4</sup>[ramprasadchegu1984@gmail.com](mailto:ramprasadchegu1984@gmail.com)

Nomenclature	
m-bipolar fuzzy graph	m-BPFG
Strongly edge irregular	SEIR
Strongly edge totally irregular	SETIR
Neighbourly edge irregular	NEIR
Neighbourly edge totally irregular	NETIR
Highly irregular	HIR

**Abstract**

In combinatory and theoretical computer science, irregular graphs are crucial. Strongly irregular graphs belong to a significant class of highly organised graphs. We define SETIR m-BPFG and SEIR m-BPFG in this study. We establish equivalence between SEIR m-BPFG and SETIR m-BPFG and investigate a few features of the former and the latter.

**Keywords:** m-BPFG, SEIR m-BPFG, SETIR m-BPFG, irregular m-BPFG

**1. Introduction**

Each of the nodes and edges of an m-polar fuzzy graph includes components, but those features are fixed. However, these elements could be bipolar. An m-BPFG has been presented based on this concept.

Bose [7] was the first to define a strongly regular graph. Regular and irregular fuzzy graphs were first proposed by Nagoorgani et al. [8, 9]. Radha and Kumaravel [10] were the ones who initially proposed the idea of a substantially regular fuzzy graph. The paper introduces the notion of strongly edge irregular and strongly edge entirely irregular m-BPFGs. Bose [7] was the first to define a strongly regular graph. Regular and irregular fuzzy graphs were first proposed by Nagoorgani et al. [8, 9]. The idea of SEIR and SETIR m-BPFGs is

introduced in this study. Additionally, certain aspects of them are investigated to define it and explored some of their characteristics.

## 2. Preliminaries

Prior to creating the m-BPFG, we presumptively consider:

Define an equivalency relation  $\leftrightarrow, N \times N - \{(r, r) : r \in N\}$  on the basis of the following  $(\gamma_1, \delta_1) \leftrightarrow (\gamma_2, \delta_2) \Leftrightarrow$  either  $(\gamma_1, \delta_1) = (\gamma_2, \delta_2)$  or  $\gamma_1 = \delta_2, \delta_1 = \gamma_2$  for a given set  $N$ .

In this case, the Quotient Set is indicated by  $\overline{N^2}$ .

**Definition 2.1:** [5] A 3-tuple  $Z = (N, A, B)$  is an m-BPFG of a graph  $Z^* = (N, E)$ , where

$A = \left\langle \left[ p_j \circ \Psi_A^p, p_j \circ \Psi_A^n \right]_{j=1}^m \right\rangle, p_j \circ \Psi_A^p : N \rightarrow [0, 1]$  and  $p_j \circ \Psi_A^n : V \rightarrow [-1, 0]$  is an m-BPFS on  $N$  and  $B = \left\langle \left[ p_j \circ \Psi_B^p, p_j \circ \Psi_B^n \right]_{j=1}^m \right\rangle, p_j \circ \Psi_B^p : \overline{N^2} \rightarrow [0, 1]$  and  $p_j \circ \Psi_B^n : \overline{N^2} \rightarrow [-1, 0]$  is an m-

BPFS in  $\overline{N^2}$  such that  $p_j \circ \Psi_B^p(\tau, \varsigma) \leq \min \{ p_j \circ \Psi_A^p(\tau), p_j \circ \Psi_A^p(\varsigma) \},$

$p_j \circ \Psi_B^n(\tau, \varsigma) \geq \max \{ p_j \circ \Psi_A^n(\tau), p_j \circ \Psi_A^n(\varsigma) \}$  for all  $(\tau, \varsigma) \in \overline{N^2}, j = 1, 2, \dots, m$  and

$p_j \circ \Psi_B^p(\tau, \varsigma) = p_j \circ \Psi_B^n(\tau, \varsigma) = 0$  for all  $(\tau, \varsigma) \in \overline{N^2} - E$ .

**Definition 2.2:** An m-BPFG node's  $\gamma \in N$  neighbourhood degree in  $Z = (N, A, B)$  is

described as  $d_{Nb}(\gamma) = \left\langle \left[ p_j \circ d_{Nb}^p(\gamma), p_j \circ d_{Nb}^n(\gamma) \right]_{j=1}^m \right\rangle = \left\langle \left[ \sum_{t \in Nb(\gamma)} p_j \circ \Psi_A^p(t), \sum_{t \in Nb(\gamma)} p_j \circ \Psi_A^n(t) \right] \right\rangle$

**Definition 2.3:** The open neighbourhood degree of a node  $\gamma \in N$  in an m-BPFG

$Z = (N, A, B)$  is defined as

$$d_Z(\gamma) = \left\langle \left[ p_j \circ d_Z^p(\gamma), p_j \circ d_Z^n(\gamma) \right]_{j=1}^m \right\rangle = \left\langle \left[ \sum_{\substack{\gamma \neq \delta \\ (\gamma, \delta) \in E}} p_j \circ \Psi_B^p(\gamma, \delta), \sum_{\substack{\gamma \neq \delta \\ (\gamma, \delta) \in E}} p_j \circ \Psi_B^n(\gamma, \delta) \right]_{j=1}^m \right\rangle$$

**Definition 2.4:** The closed neighbourhood degree of a node  $\gamma \in N$  in an m-BPFG

$Z = (N, A, B)$  is defined as

$$d_Z[\gamma] = \left\langle \left[ p_j \circ d_G^p[\gamma], p_j \circ d_G^n[\gamma] \right]_{j=1}^m \right\rangle = \left\langle \left[ \sum_{\substack{\gamma \neq \delta \\ (\gamma, \delta) \in E}} p_j \circ \Psi_B^p(\gamma, \delta), \sum_{\substack{\gamma \neq \delta \\ (\gamma, \delta) \in E}} p_j \circ \Psi_B^n(\gamma, \delta) \right]_{j=1}^m \right\rangle + \left\langle \left[ p_j \circ \Psi_A^p(\gamma), p_j \circ \Psi_A^n(\gamma) \right]_{j=1}^m \right\rangle$$

**Definition 2.5:** If all of the nodes have the same open neighbourhood degree  $\langle [\eta_j^p, \eta_j^n]_{j=1}^m \rangle,$

then an m-BPFG  $Z$  of  $Z^*$  is said to be  $\langle [\eta_j^p, \eta_j^n]_{j=1}^m \rangle$ -regular.

**Definition 2.6:** If all of the nodes have the same closed neighbourhood degree  $\langle [\gamma_j^p, \gamma_j^n]_{j=1}^m \rangle,$  then an m-BPFG  $Z$  of  $Z^*$  is said to be  $\langle [\gamma_j^p, \gamma_j^n]_{j=1}^m \rangle$ -totally regular.

**Definition 2.7:** An m-BPFG  $Z$  of  $Z^*$  is said to be irregular if there exists a node which is adjacent to node with different degree.

### 3. Irregular graphs

In this section some irregular graphs are discussed.

**Definition 3.1:** Let  $Z$  of  $Z^*$  be an m- BPFG. Then  $Z$  is said to be HIR m-BPFG if each node of  $Z$  is adjacent to nodes with different degrees.

**Definition 3.2:** Let  $Z$  be an m-BPFG. Then  $Z$  is said to be NEIR m-BPFG if each pair of adjacent edges have different degrees.

**Definition 3.3:** Let  $Z$  be an m- BPFG. Then  $Z$  is said to be NETIR m-BPFG if each pair of adjacent edges have different total degrees.

**Definition 3.4:** Let  $Z$  be an m-BPFG. Then

(i) If each pair of edges has a different degree, then  $Z$  is called **SEIR** m-BPFG. (i.e. no two edges have the equal degree) [5].

(ii) If each pair of edges has a different total degree, then  $Z$  called **SETIR** m-BPFG. (i.e. no two edges have the equal degree) [5].

**Theorem 3.1:** Let  $Z = (N, A, B)$  be an m-BPFG of  $Z^*$  where  $B$  is constant. Then  $Z$  is SEIR m-BPFG if and only if  $Z$  is SETIR m-BPFG.

**Proof:** Let  $B(\gamma, \delta) = \left\langle [p_j \circ \psi_B^p(\gamma, \delta), p_j \circ \psi_B^n(\gamma, \delta)]_{j=1}^m \right\rangle = \left\langle [k_j^p, k_j^n]_{j=1}^m \right\rangle$  for all  $(\gamma, \delta) \in E$ , where  $k_j^p \in [0,1]$  and  $k_j^n \in [-1,0]$ .

Let  $Z$  be SEIR m-BPFG.

$$\Leftrightarrow d_z(\gamma_1, \gamma_2) \neq d_z(\delta_1, \delta_2) \text{ for all } (\gamma_1, \gamma_2), (\delta_1, \delta_2) \in E$$

$$\Leftrightarrow d_z(\gamma_1, \gamma_2) + \left\langle [k_j^p, k_j^n]_{j=1}^m \right\rangle \neq d_z(\delta_1, \delta_2) + \left\langle [k_j^p, k_j^n]_{j=1}^m \right\rangle \text{ for all } (\gamma_1, \gamma_2), (\delta_1, \delta_2) \in E$$

$$\Leftrightarrow d_z(\gamma_1, \gamma_2) + B(\gamma_1, \gamma_2) \neq d_z(\delta_1, \delta_2) + B(\delta_1, \delta_2) \text{ for all } (\gamma_1, \gamma_2), (\delta_1, \delta_2) \in E$$

$$\Leftrightarrow td_z(\gamma_1, \gamma_2) \neq td_z(\delta_1, \delta_2) \text{ for all } (\gamma_1, \gamma_2), (\delta_1, \delta_2) \in E$$

$$\Leftrightarrow Z \text{ is SETIR m-BPFG.}$$

**Remark 3.1:**  $B$  might not be a constant function if  $Z = (N, A, B)$  is both SEIR and SETIR m-BPFG.

**Theorem 3.2:** If  $Z$  is SEIR m-BPFG, then  $Z$  is NEIR m-BPFG.

**Proof:** As  $Z$  is SEIR m-BPFG, therefore each pair of edges in  $Z$  have different degrees. Hence each pair of adjacent edges have different degrees.

So,  $Z$  is NEIR m-BPFG.

**Theorem 3.3:** If  $Z$  is SETIR-BPFG, then  $Z$  is NETIR m-BPFG.

**Proof:** Let  $Z$  be an m-BPFG and SETIR.

Each pair of edges in  $Z$  has a different total degree, hence each pair of adjacent edges also has a different total degree, making  $Z$  a NETIR m-BPFG.

**Theorem 3.4:** Let  $Z = (N, A, B)$  be an m-BPFG of  $Z^*$  where  $B$  is constant. If  $Z$  is SEIR m-BPFG, then  $Z$  is an irregular m-BPFG.

**Proof:** Let  $B(\gamma, \delta) = \left\langle [p_j \circ \psi_B^p(\gamma, \delta), p_j \circ \psi_B^n(\gamma, \delta)]_{j=1}^m \right\rangle = \left\langle [k_j^p, k_j^n]_{j=1}^m \right\rangle$  for all  $(\gamma, \delta) \in E$

,where  $k_j^p \in [0, 1]$  and  $k_j^n \in [-1, 0]$ . As  $Z$  is SEIR, we have each pair of edges will have different degrees. Assume that the two adjacent edges  $(\gamma_1, \delta_1)$  and  $(\delta_1, \eta_1)$  having distinct degrees.

$$\begin{aligned} & \text{This provides that } d_Z(\gamma_1, \delta_1) \neq d_Z(\delta_1, \eta_1) \\ & \Rightarrow d_Z(\gamma_1) + d_Z(\delta_1) - 2 \left\langle \left[ p_j \circ \psi_B^p(\gamma_1, \delta_1), p_j \circ \psi_B^n(\gamma_1, \delta_1) \right]_{j=1}^m \right\rangle \neq \\ & d_Z(\delta_1) + d_Z(\eta_1) - 2 \left\langle \left[ p_j \circ \psi_B^p(\delta_1, \eta_1), p_j \circ \psi_B^n(\delta_1, \eta_1) \right]_{j=1}^m \right\rangle \\ & d_Z(\gamma_1) + d_Z(\delta_1) - 2 \left\langle \left[ k_j^p, k_j^n \right]_{j=1}^m \right\rangle \neq d_Z(\delta_1) + d_Z(\eta_1) - 2 \left\langle \left[ k_j^p, k_j^n \right]_{j=1}^m \right\rangle \\ & \Rightarrow d_Z(\gamma_1) \neq d_Z(\eta_1). \end{aligned}$$

This indicates that the node  $\delta_1$  that is adjacent to the nodes  $\gamma_1$  and  $\eta_1$  have different degrees.

As a result,  $Z$  is irregular.

**Theorem 3.5:** Let  $Z = (N, A, B)$  be an m-BPFG of  $Z^*$  where  $B$  is constant. If  $Z$  is SEIR m-BPFG then  $Z$  is HIR m-BPFG.

**Proof:** Let  $B(\alpha, \beta) = \left\langle \left[ p_j \circ \psi_B^p(\alpha, \beta), p_j \circ \psi_B^n(\alpha, \beta) \right]_{j=1}^m \right\rangle = \left\langle \left[ k_j^p, k_j^n \right]_{j=1}^m \right\rangle$  for all  $(\alpha, \beta) \in E$ , where  $k_j^p \in [0, 1]$  and  $k_j^n \in [-1, 0]$ . Assume that  $\alpha_2$  be any node adjacent with the nodes  $\alpha_1, \alpha_3$  and  $\alpha_4$ . Thus  $(\alpha_1, \alpha_2), (\alpha_2, \alpha_3), (\alpha_2, \alpha_4)$  are adjacent edges in  $Z$ . Let us consider that  $Z$  is SEIR m-BPFG. Thus each pair of edges in  $Z$  have different degrees. Hence, each pair of adjacent edges in  $Z$  have different degrees.

$$\begin{aligned} & \text{Hence, } d_Z(\alpha_1, \alpha_2) \neq d_Z(\alpha_2, \alpha_3) \neq d_Z(\alpha_2, \alpha_4) \\ & \Rightarrow d_Z(\alpha_1) + d_Z(\alpha_2) - 2 \left\langle \left[ p_j \circ \psi_B^p(\alpha_1, \alpha_2), p_j \circ \psi_B^n(\alpha_1, \alpha_2) \right]_{j=1}^m \right\rangle \neq \\ & d_Z(\alpha_2) + d_Z(\alpha_3) - 2 \left\langle \left[ p_j \circ \psi_B^p(\alpha_2, \alpha_3), p_j \circ \psi_B^n(\alpha_2, \alpha_3) \right]_{j=1}^m \right\rangle \neq \\ & d_Z(\alpha_2) + d_Z(\alpha_4) - 2 \left\langle \left[ p_j \circ \psi_B^p(\alpha_2, \alpha_4), p_j \circ \psi_B^n(\alpha_2, \alpha_4) \right]_{j=1}^m \right\rangle \\ & \Rightarrow d_Z(\alpha_1) + d_Z(\alpha_2) - 2 \left\langle \left[ k_j^p, k_j^n \right]_{j=1}^m \right\rangle \neq d_Z(\alpha_2) + d_Z(\alpha_3) - 2 \left\langle \left[ k_j^p, k_j^n \right]_{j=1}^m \right\rangle \neq \\ & d_Z(\alpha_2) + d_Z(\alpha_4) - 2 \left\langle \left[ k_j^p, k_j^n \right]_{j=1}^m \right\rangle \\ & \Rightarrow d_Z(\alpha_1) \neq d_Z(\alpha_3) \neq d_Z(\alpha_4). \end{aligned}$$

Hence the node  $\alpha_2$  is adjacent to the nodes  $\alpha_1, \alpha_3$  and  $\alpha_4$  with different degrees.

As a result,  $Z$  is HIR.

#### 4. Some Properties of Neighbourly Edge Totally Irregular m-BPFGs

In this part, we look at a few SETIR m-BPFG and NETIR m-BPFG features.

**Definition 4.1:** A walk in a directed graph  $\vec{Z} = (\vec{N}, E)$  is a series of steps  $w = v_1 \vec{e}_1 v_2 \vec{e}_2 \cdots v_{k-1} \vec{e}_{k-1} v_k$  of nodes  $v_i$  and arcs  $\vec{e}_i$  of  $\vec{Z}$  such that the head and tail of  $\vec{e}_i$  are  $v_i$  and  $v_{i+1}$  for all  $i = 1, 2, \dots, k-1$  respectively. If  $v_1 = v_k$ , then a walk is said to be closed. A walk with different arcs is called a trail. A walk with different nodes is called a path. If  $v_1 = v_k$ , then the path  $v_1, v_2, \dots, v_k$  with  $k \geq 3$  is a cycle. The number of edges on a path or cycle determines its length.

**Definition 4.2:** If every edge of an m-BPFG  $Z = (N, A, B)$  of  $Z^*$  is having the equal total degree  $\langle [\delta_j^p, \delta_j^n]_{j=1}^m \rangle$ , thus  $Z$  is said to be totally edge regular m-BPFG.

**Property 4.1:** Let  $Z = (N, A, B)$  be an m-BPFG of  $Z^*$  and  $B$  is constant. If  $Z$  is SETIR m-BPFG, thus  $Z$  is HIR m-BPFG.

**Property 4.2:** Let  $Z = (N, A, B)$  be an m-BPFG of  $Z^*$  that is a path of  $2r$  ( $r > 1$ ) nodes.

If the membership value of the edges  $f_1, f_2, \dots, f_{2r-1}$  are

$\left( [b_j^{p(1)}, b_j^{n(1)}]_{j=1}^m \right), \left( [b_j^{p(2)}, b_j^{n(2)}]_{j=1}^m \right), \dots, \left( [b_j^{p(2r-1)}, b_j^{n(2r-1)}]_{j=1}^m \right)$  respectively such that  $b_j^{p(1)} < b_j^{p(2)} < \dots < b_j^{p(2r-1)}$  and  $b_j^{n(1)} > b_j^{n(2)} > \dots > b_j^{n(2r-1)}$ , then  $Z$  is both SEIR and SETIR.

(Here,  $f_i = v_i v_{i+1}$  for  $i = 1, 2, \dots, (2r-1)$ ).

**Theorem 4.1:** Let  $Z = (N, A, B)$  be an m-BPFG of  $Z^*$  that is a path of cycle

$r$  ( $r \geq 4$ ) nodes. If the membership value of the edges  $f_1, f_2, \dots, f_r$  are

$\left( [b_j^{p(1)}, b_j^{n(1)}]_{j=1}^m \right), \left( [b_j^{p(2)}, b_j^{n(2)}]_{j=1}^m \right), \dots, \left( [b_j^{p(r)}, b_j^{n(r)}]_{j=1}^m \right)$  respectively such that  $b_j^{p(1)} < b_j^{p(2)} < \dots < b_j^{p(r)}$ ,  $b_j^{n(1)} > b_j^{n(2)} > \dots > b_j^{n(r)}$ , then  $Z$  is both SEIR and SETIR.

**Proof:** Let  $f_1, f_2, \dots, f_r$  be the edges of the cycle  $Z^*$  in that order.

Thus, we get

$$d_Z(v_i) = \left( [b_j^{p(i-1)} + b_j^{p(i)}, b_j^{n(i-1)} + b_j^{n(i)}]_{j=1}^m \right) \text{ for } i = 2, 3, \dots, r \text{ and}$$

$$d_Z(v_1) = \left( [b_j^{p(1)} + b_j^{p(r)}, b_j^{n(1)} + b_j^{n(r)}]_{j=1}^m \right),$$

$$d_Z(f_i) = \left( [b_j^{p(i-1)} + b_j^{p(i+1)}, b_j^{n(i-1)} + b_j^{n(i+1)}]_{j=1}^m \right) \text{ for } i = 2, 3, \dots, (r-1),$$

$$d_Z(f_1) = \left( [b_j^{p(2)} + b_j^{p(r)}, b_j^{n(2)} + b_j^{n(r)}]_{j=1}^m \right),$$

$$d_Z(f_r) = \left( [b_j^{p(1)} + b_j^{p(r-1)}, b_j^{n(1)} + b_j^{n(r-1)}]_{j=1}^m \right)$$

So,  $Z$  is SEIR m-BPFG.

Again, since

$$td_Z(f_i) = \left( [b_j^{p(i-1)} + b_j^{p(i+1)} + b_j^{p(i)}, b_j^{n(i-1)} + b_j^{n(i+1)} + b_j^{n(i)}]_{j=1}^m \right) \text{ for } i = 2, 3, \dots, (r-1),$$

$$td_Z(f_1) = \left( \left[ b_j^{p(2)} + b_j^{p(1)} + b_j^{p(r)}, b_j^{n(2)} + b_j^{n(1)} + b_j^{n(r)} \right]_{j=1}^m \right),$$

$$td_Z(f_r) = \left( \left[ b_j^{p(1)} + b_j^{p(r)} + b_j^{p(r-1)}, b_j^{n(1)} + b_j^{n(r)} + b_j^{n(r-1)} \right]_{j=1}^m \right),$$

as a result,  $Z$  is SETIR m-BPFG.

**Theorem 4.2:** Let  $Z = (N, A, B)$  be an m-BPFG of  $Z^*$  that is a star  $K_{1,r}$ . If There are no two edges with the same membership values, thus  $Z$  is both SEIR and totally edge regular m-BPFG.

**Proof:** Let the nodes adjacent to the node  $l_0$  be  $l_1, l_2, \dots, l_r$ . Let the edges of the star  $Z^*$  be  $f_1, f_2, \dots, f_r$ , with the membership values

$$\left( \left[ b_j^{p(1)}, b_j^{n(1)} \right]_{j=1}^m \right), \left( \left[ b_j^{p(2)}, b_j^{n(2)} \right]_{j=1}^m \right), \dots, \left( \left[ b_j^{p(r)}, b_j^{n(r)} \right]_{j=1}^m \right) \text{ such that}$$

$$\left( \left[ b_j^{p(1)}, b_j^{n(1)} \right]_{j=1}^m \right) \neq \left( \left[ b_j^{p(2)}, b_j^{n(2)} \right]_{j=1}^m \right) \neq \dots \neq \left( \left[ b_j^{p(r)}, b_j^{n(r)} \right]_{j=1}^m \right). \text{ Then}$$

$$d_Z(f_i = (l_0, l_i)) = d_Z(l_0) + d_Z(l_i) - 2B(l_0, l_i)$$

$$= \left( \left[ b_j^{p(1)} + b_j^{p(2)} + \dots + b_j^{p(r)}, b_j^{n(1)} + b_j^{n(2)} + \dots + b_j^{n(r)} \right]_{j=1}^m + \left[ b_j^{p(i)}, b_j^{n(i)} \right] - 2 \left[ b_j^{p(i)}, b_j^{n(i)} \right] \right)$$

$$= \left( \left[ b_j^{p(1)} + b_j^{p(2)} + \dots + b_j^{p(r)}, b_j^{n(1)} + b_j^{n(2)} + \dots + b_j^{n(r)} \right]_{j=1}^m - \left[ b_j^{p(i)}, b_j^{n(i)} \right] \right) \text{ for } i = 1, 2, \dots, r.$$

All of the edges' degrees can be seen to vary.  $Z$  is hence SEIR.

Also  $td_Z(f_i = (l_0, l_i))$

$$= \left( \left[ b_j^{p(1)} + b_j^{p(2)} + \dots + b_j^{p(r)}, b_j^{n(1)} + b_j^{n(2)} + \dots + b_j^{n(r)} \right]_{j=1}^m - \left[ b_j^{p(i)}, b_j^{n(i)} \right] + \left[ b_j^{p(i)}, b_j^{n(i)} \right] \right)$$

$$= \left( \left[ b_j^{p(1)} + b_j^{p(2)} + \dots + b_j^{p(r)}, b_j^{n(1)} + b_j^{n(2)} + \dots + b_j^{n(r)} \right]_{j=1}^m \right) \text{ for } i = 1, 2, \dots, r.$$

As a result,  $Z$  is totally edge regular because all of the edges have the same total number of degree.

### Conclusions

We introduce and investigate the idea of SEIR and SETIR m-BPFGs. SETIR and SEIR m-BPFGs are described. Researchers have looked into a number of their crucial characteristics.

### References

- [1] Akram M. Bipolar fuzzy graphs, *Information Sciences*, 181(2011)5548-5564.
- [2] Bhutani, K.R., Moderson, J., Rosenfeld, A.: On degrees of end nodes and cut nodes in fuzzy graphs. *Iran. J. Fuzzy Syst.* 1(1), 57–64 (2004).
- [3] Ghorai G. and Pal M. Some isomorphic properties of m-polar fuzzy graphs with Applications, *Springer plus*, 5(2016) 1-21.

- [4] GHORAI G. AND PAL M, "NOVEL CONCEPTS OF SEIR  $m$ -POLAR FUZZY GRAPHS" INTERNATIONAL JOURNAL OF APPLIED AND COMPUTATIONAL MATHEMATICS, VOL. 3, 2017, 3321–3332.
- [5] Ramakrishna Mankena, T.V. Pradeep Kumar, Ch. Ramprasad and J. VijayaKumar, "Edge Regularity on  $m$ -BPPFG", Annals of Pure and Applied Mathematics Vol. 23, No. 1, 2021, 27-36.
- [6] Ramakrishna Mankena, T.V. Pradeep Kumar, Ch. Ramprasad and K. V. RangaRao , "Neighborhood Degrees Of  $m$ -Bipolar Fuzzy Graph", J. Math. Comput. Sci. 11 (2021), No. 5, 5614-5628.
- [7] R. Bose, Strongly regular graphs, partial geometries and partially balanced designs, Pacific Journal of Mathematics, 13(2) 389-419 (1963).
- [8] A. Nagoorgani and K. Radha, On regular fuzzy graphs, Journal of Physical Sciences, 12 33-40 (2008).
- [9] A. Nagoorgani and A. Latha, On irregular fuzzy graphs, Applied Mathematical Sciences, 6(11) 517-523 (2012).
- [10] K. Radha and N. Kumaravel, On edge regular fuzzy graphs, International Journal of Mathematical Archive, 5(9) 100-112 (2014).